

**ERRATA: “POST-MODERN ALGEBRA,”  
SMITH & ROMANOWSKA**

**Line 3–12:** iff there is a basis  $D$  of  $W$  extending  $f(B)$  such that

**Line 10+7:**  $\Sigma\langle A_i \mid i \in I \rangle$

**Line 10+8:**  $\bigcup\{\{i\} \times A_i \mid i \in I\}$

**Line 10+10:**  $\iota_i p = p_i$

**Line 10+11:**  $\Pi\langle A_i \mid i \in I \rangle$

**Line 14+14:**  $|f_n(x) - f_m(x)|$

**Line 20+5:** Define  $\langle X \rangle = \bigcup_{n \in \mathbb{N}} X^n$ .

**Line 21+3:** subset  $C$  of  $A^+$  is a *code*

**Line 26+4:**  $A^2 = \alpha_1 \circ \alpha_2$

**Line 26–16ff:** Let  $\alpha_1, \alpha_2, \alpha_3$  be equivalence relations on a set  $A$ .

Define  $\beta_i = \alpha_j \cap \alpha_k$  for  $\{i, j, k\} = \{1, 2, 3\}$ . Suppose that the set  $\{\alpha_i, \beta_i \mid 1 \leq i \leq 3\}$  is permutable, with  $\alpha_i \circ \beta_i = A^2$  for  $1 \leq i \leq 3$ . If  $\alpha_1 \cap \alpha_2 \cap \alpha_3 = \hat{A}$ , show that  $A$  is the direct product  $A^{\alpha_1} \times A^{\alpha_2} \times A^{\alpha_3}$ .

**Line 30–14:** Exercise 1A

**Line 31+10:** operations  $m_{A \cup B} =$

**Line 31–15:**  $\prod_{1 \leq i \leq 2} (A_i, M)$

**Line 33+12:**  $\chi : A \rightarrow 2^M; x \mapsto L_x^{-1}(B)$

**Page 35, diagram:** Reverse the direction of the arrow between  $h_1$  and  $h_0$

**Line 39+2:**  $\langle T \rangle; m \mapsto (m, m)$ .

**Line 40+15:**  $\iota_b p = p_b$

**Line 44–13:**  $(G, H^{\text{OP}}) \cong \sum_{H \setminus G} (H, H^{\text{OP}})$

**Line 46–3:** A set map  $f : X \rightarrow M$

**Line 49+17:** homomorphism

**Line 57+11:**  $\text{Mlt}(Q, \cdot)$

**Line 58+4:** writing e.g.  $(A, B, C, V)$

**Line 58+20:**

$$T = \prod_i (x_i, x_i T, \dots, x_i T^{n_i-1})$$

**Line 58–4:**

$$(C \xrightarrow{L(C)} C \xrightarrow{L(V)} V \xrightarrow{L(C)} B \xrightarrow{L(V)} C)$$

**Line 62–14:** 2.2E.

**Line 64–8:** and  $(X, H) \uparrow_H^G \cup (Y, H) \uparrow_H^G$  are

**Line 68+18:**

$$(X \cup X^J)^* \xrightarrow{R} XG \xrightarrow{p} \mathbb{Z}_2$$

**Line 71+6:**  $p^m = 1 + \sum_{i=2}^s |t_i G_e|$ ,

**Line 73+10:**

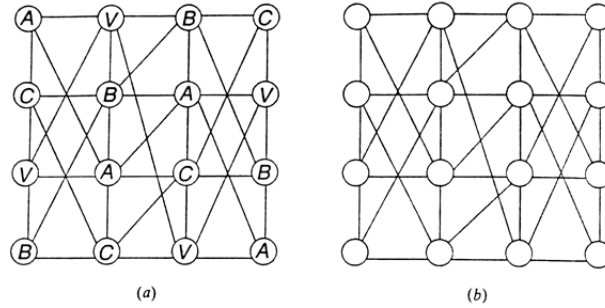
$$x - y$$

**Line 85-6:**  $= \frac{1}{2}n \cdot (n-1)! = \frac{1}{2}n! =$

**Line 87-6:**  $x \setminus y = e \cdot ((x/(e \setminus e)) \setminus y)$

**Line 88+8:** Let  $(N, \langle \alpha_i \mid 1 \leq i \leq k \rangle)$  be a  $k$ -net.

**Page 89:** Figure 1.2(b) should have the same diagonal lines as Figure 1.2(a).

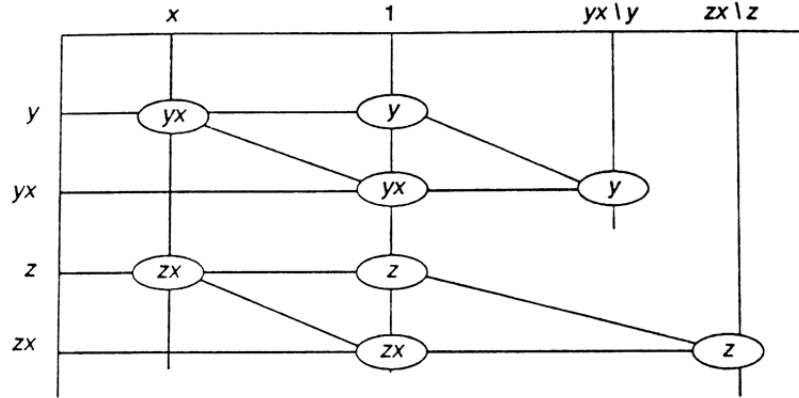


**Line 91-12:**  $(Q, \cdot, /, \setminus) \rightarrow (Q, \cdot, /, \setminus)$  from  $Q$

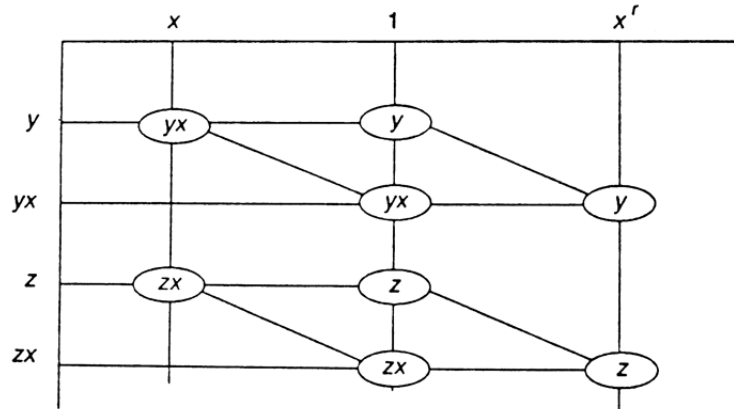
**Line 93+14:**

$$I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}.$$

**Page 97:** Add diagonal lines connecting the following pairs of ellipses in each of (a), (b) of Figure 1.3:  $yx, y, zx, z$ .



(a)



(b)

**Page 98:** Should be  $x(zy \cdot z)$  in the ellipse at row  $x$ , column  $zy \cdot z$ .

**Line 101+6:** Define  $x \cdot y = x = x/y$  for

**Line 103–10:** Show that  $(Q, /, \cdot)$

**Line 118–14:** if  $y = x$  then  $a$  else  $0$

**Line 121–6:**

$$\rho_T = \sum_{i=1}^n \pi_i \iota_{iT} \in \text{End} \bigoplus_{i=1}^n A.$$

**Line 127+16:** non-trivial unital ring

**Line 128–6:**  $l_i \in L \} \triangleleft S$ .

**Line 128–4:** (c) For distinct  $K, L \in \text{Spec}(\mathbb{Z})$ ,

**Line 129+2:** If  $S$  is unital, nontrivial and

**Line 140+3:**  $\subseteq S_1^l \Rightarrow xA = b \Rightarrow xA_0 = xAE = bE = b_0$

**Line 143+5:** for some  $0 \leq r \leq \min\{l, m\}$  and

**Line 143+12ff:** Otherwise, one may pick  $x_{r+1}, \dots, x_l$  to be arbitrary members of the field  $S$  (so the system is under-determined if  $r < l$ ), and then use the first  $r$  equations of the reduced system to obtain  $x_1, \dots, x_r$  in terms of  $b'_1, \dots, b'_r$  and possibly  $x_{r+1}, \dots, x_l$ .

**Page 147, (2.3.6):**

$$\begin{array}{ccc} I & \xrightarrow{f} & V \\ \theta \downarrow & & \downarrow \tilde{\theta} \\ W & \xlongequal{\quad} & W \end{array}$$

**Line 150–1:**  $T : h \mapsto (Th : (v_1, \dots, v_n) \mapsto h(v_{1T}, \dots, v_{nT}))$

**Line 151+13:**

$$h \mapsto \left( \sum_{i=1}^n \theta \right) h.$$

**Line 151–5:**

$$= k \det \left( \sum_{j_1=1}^n f_{1j_1} E_{1n}^{1j_1}, \dots \right)$$

**Line 162+17ff: 3B.** Let  $A$  be a nontrivial  $K$ -module. Let  $M$  be the subset of  $K(A, A; A)$  consisting of those bilinear maps  $m : A \times A \rightarrow A$  for which  $(A_K, m, 1)$  is a  $K$ -algebra. Show that  $M$  is not a submodule of  $K(A, A; A)$ .

**Line 163+7:**  $T\bar{\theta} = T\theta$ .

**Line 163–3:** is a submonoid of the monoid  $(\mathbb{R}[T_1, \dots, T_n], \cdot, 1)$ .

**Line 164–13:** under the action  $M \times A \times K \rightarrow M \times A; (m, a, k) \mapsto (m, ak)$ ,

**Line 169–15:** Since  $a$  is

**Line 170+7:** coset  $f(T) + d(T) \cdot K[T]$

**Line 170–18:** morphism  $K[T] \rightarrow K$

**Lines 170–3, 170–2, 171+2:**  $(\text{Max } A)^{*k}$

**Line 171+14, 15:** If  $a_1 A$  is proper,

**Line 172+2:** subsemigroup of  $(K[T], \cdot)$ .

**Line 173–5:** show that each non-zero prime ideal is maximal.

**Line 174+5:**  $\mapsto \det f$  is

**Line 177–18:**  $A^m \cong \bigoplus_{i=1}^m$

**Line 183–13:** Now  $d_m K[T]$

**Line 183–11:** mial  $d_m$  is called

**Line 184+8:** *polynomial of an endomorphism is its last invariant factor,*

**Line 188–13:** Moreover,  $L = K(a)$ .

- Line 189–11:** polynomial  $T^{d_m} - 1$  in  $K[T]$   
**Line 189–10:**  $n = d_m$   
**Line 196–13:**  $(K^\alpha, *, \delta)$   
**Line 197–16:** disjoint union  $\bigcup_{X, Y \in \underline{\text{Set}}_0}$   
**Line 198+4:** Example 1.6(b).  
**Line 209–1:**  $YS$  in bottom, left-hand corner of (1.4.2).  
**Line 209–1:**  $YS$  in bottom, left-hand corner of (1.4.2).  
**Line 223–12:**  $\text{Fix}(2^X, \langle T \rangle)$   
**Line 243+6:**  $\varinjlim F$   
**Line 263+14:** with  $B < D < C$ ,  
**Line 264+18:** In the image Example 3.3.2(b), consider the case  
 where  $f$  surjects.  
**Line 265+6:** Monarchy?  
**Line 284+14:**  $(A, \cdot, /, 1)$   
**Line 288–8:**  $\text{nat } \alpha :$   
**Line 308–3:**  $\bar{h} : X\Omega R_{\underline{K}} \rightarrow A$   
**Line 314–1:**  $P\Omega$  in bottom, left-hand corner of diagram  
**Line 363–16l:** Frobenius homomorphism, 188  
**Line 363–16r:** Heyting algebra, 267  
**Line 365–19r:** monoid ring functor  
**Line 370–3l:**  $\widehat{V}$ , 327