

**MATH 201 SPRING 2023 GRADED HOMEWORK #1**

*Write clearly. Both questions carry equal weight.*

For each proposition, write a formal proof.

(1) For real  $x$  with  $0 < x < 6$ , the inequality  $\frac{9}{x(6-x)} \geq 1$  holds.

(2) Consider integers  $m$  and  $n$ . For  $m^2 + mn + n^2$  to be odd,  
it is sufficient that the two integers have opposite parity.