MATH 201 SPRING 2022 PRACTICE FINAL

Write clearly, on separate paper. All questions carry equal weight. You will receive credit for your five best answers.

(1) Prove or disprove:

Let A, B, and C be subsets of a set U. Then $(\overline{A} \cup B) \cap (\overline{B} \cup C) \subseteq \overline{A} \cup C$.

(2) Prove or disprove:

The inequality $9x^2 + 16y^2 \ge 24xy$ holds for all real numbers x and y.

(3) Prove or disprove:

For each positive integer n, the integer $n^5 + 5n^3 - 6n$ is a multiple of 5.

(4) Prove or disprove:

For a real number x > -1 and a positive integer n, $(1+x)^n \ge 1 + nx$.

(5) Prove or disprove:

If a monotonic sequence $\{x_n\}$ has a bounded subsequence, then $\{x_n\}$ converges.

(6) Prove or disprove:

The series

$$\sum_{n=5}^{\infty} \frac{2n}{n^2 - 3n - 4}$$

converges.