MATH 201 FALL 2023 PRACTICE TEST #1

Write clearly, on separate paper. All questions carry equal weight. You will receive credit for your three best answers.

Prove or disprove three of the following statements:

(1) For subsets A, B, C of a universe U, one has

$$A \smallsetminus (B \cap C) = (A \smallsetminus B) \cup (A \smallsetminus C).$$

- (2) For integers x and y, if 4x 5y is even, then x and y have the same parity.
- (3) If p and r are integers, and p is prime, then

$$p \mid \binom{p}{r}$$

when 0 < r < p.

(4) If x and y are positive real numbers, then

$$xy \le \frac{1}{4}x^2 + y^2.$$